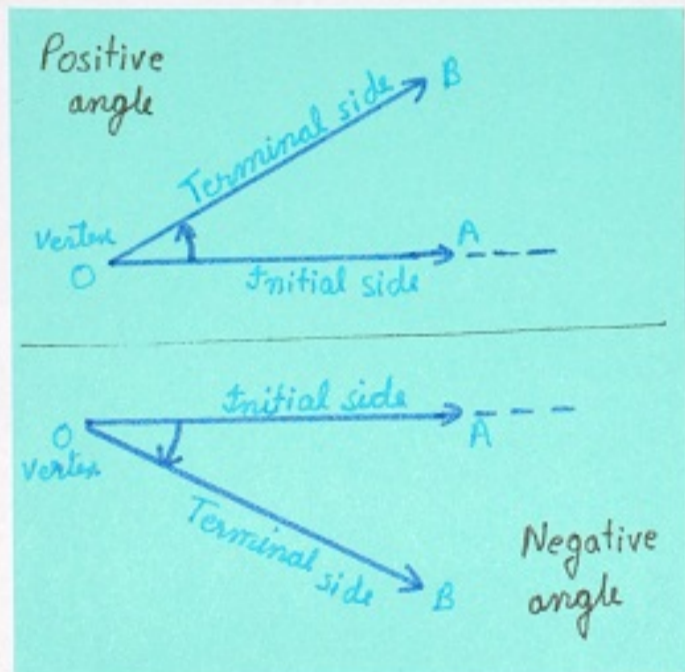


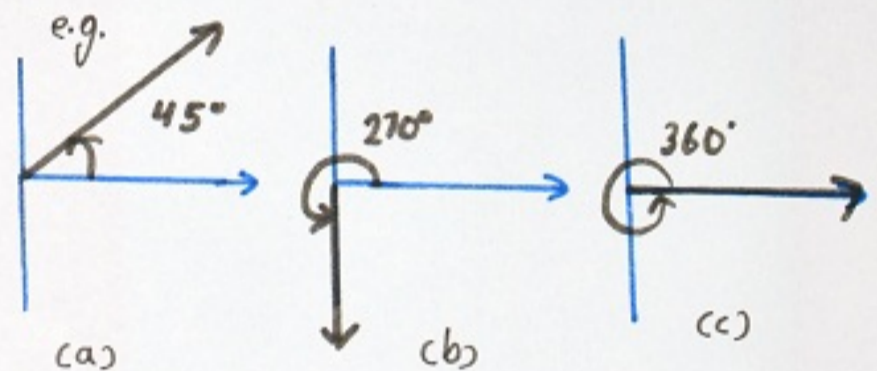
CHAPTER - 3

TRIGONOMETRIC FUNCTIONS

Angle is a measure of rotation of a given ray about its initial point (the vertex)



The measure of an angle is the amount of rotation performed to get the terminal side from the initial side.



degree measure

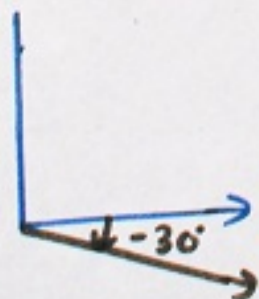
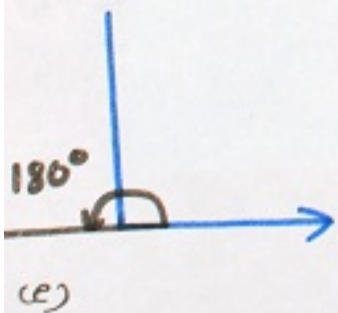
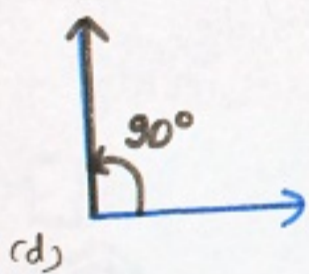
We say that if initial side = terminal side, i.e. the ray performs a complete revolution and returns to its original position,

it has moved by 360 degrees. (fig (c) above)

$$\therefore 1 \text{ degree} \equiv 1^\circ = \left(\frac{1}{360}\right)^{\text{th}} \text{ of a revolution}$$

We subdivide a degree into minutes & seconds:

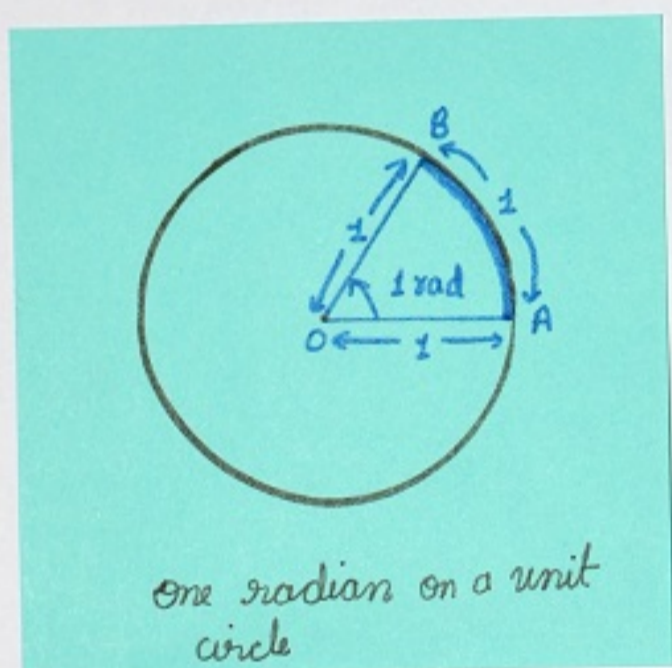
$$\begin{aligned} 1^\circ &= 60' && (60 \text{ minutes}) \\ 1' &= 60'' && (60 \text{ seconds}) \\ \therefore 1^\circ &= 60' = 3600'' && (3600 \text{ seconds}) \end{aligned}$$



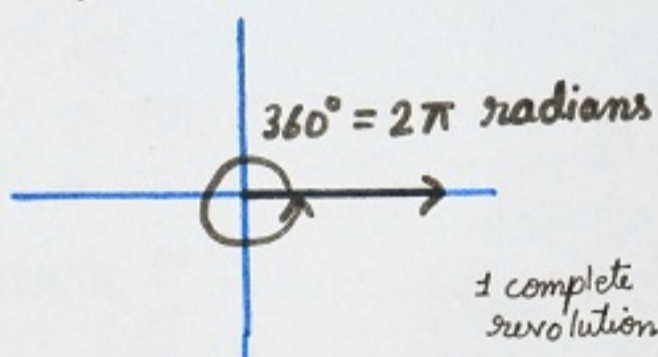
Radian measure

Radian is another measuring unit for angles. It is used as a standard instead of degrees in scientific measurements.

1 radian \equiv the angle subtended by an arc of length 1 unit in a unit circle (of radius 1) at the centre



Another way to understand it is that one complete revolution of the initial side is equivalent to angle of 2π radians:



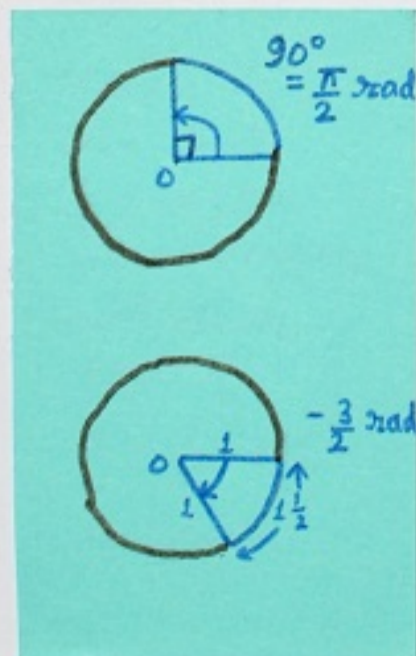
Equal arcs of a circle subtend equal angle at the centre.

In general,

$$\underline{360 \text{ degrees} \equiv 2\pi \text{ radians}} \\ \underline{\equiv 1 \text{ revolution}}$$

$$1 \text{ rad} = \frac{180}{\pi} \\ = 57^{\circ}16' \\ (\text{approx})$$

$$1^{\circ} = \frac{\pi}{180} \text{ radian} \\ = 0.01746 \text{ rad} \\ (\text{approx})$$



In a circle of radius r , an arc of length l will subtend an angle of θ radians at the centre, and we have

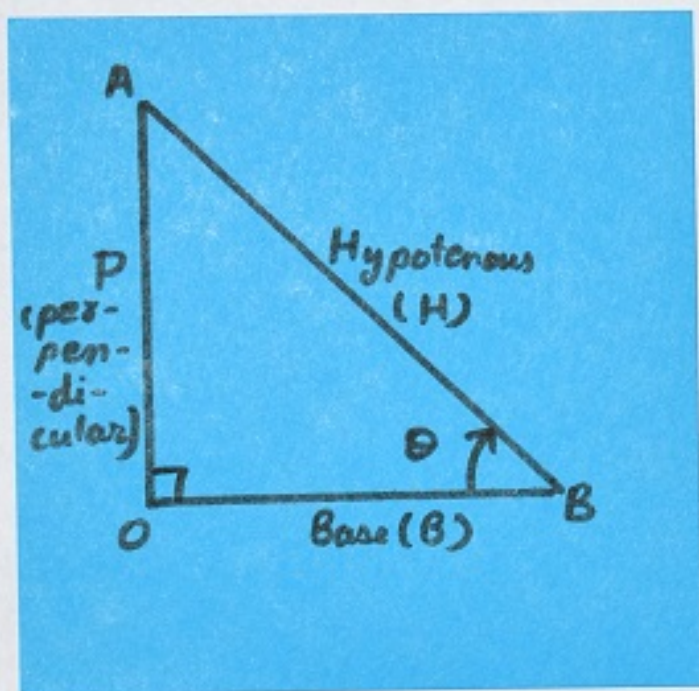
$$\theta = \frac{l}{r} \Rightarrow \boxed{l = r\theta}$$

| | | | | | | | |
|--------|-----------------|-----------------|-----------------|-----------------|-------|------------------|--------|
| DEGREE | 30° | 45° | 60° | 90° | 180° | 270° | 360° |
| RADIAN | $\frac{\pi}{6}$ | $\frac{\pi}{4}$ | $\frac{\pi}{3}$ | $\frac{\pi}{2}$ | π | $\frac{3\pi}{2}$ | 2π |

$$\text{Radian measure} = \frac{\pi}{180} \times \text{Degree measure}$$

$$\text{Degree measure} = \frac{180}{\pi} \times \text{Radian measure}$$

TRIGONOMETRIC FUNCTIONS



Let's consider an example of an acute right angled triangle OAB

We define trigonometric ratios

$$\text{as } \begin{aligned} \sin \theta &= \frac{P}{H} & , \operatorname{cosec} \theta &= \frac{H}{P} \\ \cos \theta &= \frac{B}{H} & , \sec \theta &= \frac{H}{B} \\ \tan \theta &= \frac{P}{B} & , \cot \theta &= \frac{B}{P} \end{aligned}$$

Recall that

$$P^2 + B^2 = H^2 \quad (\text{Pythagoras theorem})$$